Physics 8660, Fall 2008 Homework 5, 10/30/2008, due 11/24/2008

1 Acoustical wave guides

Density displacements $\psi(\vec{r},t)$ for a gas in a confined volume satisfy a wave equation of

the form $\frac{1}{c^2} \frac{\partial^2 \psi}{\partial t^2} - \nabla^2 \psi = 0$, $\frac{\partial \psi}{\partial n} = 0$, where c is the sound velocity and $\partial \psi / \partial n = \hat{n} \nabla \psi$ is

the normal derivative at a boundary surface.

a) Evaluate the normal modes for a long rectangular wave guide with cross sectional dimensions a x b. Show that for most modes there is a minimum frequency for transmission. Compare the phase and group velocities.

a) Evaluate the normal modes for a long cylindrical wave guide with cross sectional radius R. Show that for most modes there is a minimum frequency for transmission. Compare the phase and group velocities.

2. Acoustic modes

Sound waves in a confined volume satisfy a wave equation of the form

 $\frac{1}{v^2}\frac{\partial^2 \psi}{\partial t^2} - \nabla^2 \psi = 0, \frac{\partial \psi}{\partial n} = 0 \text{ where c is the sound velocity and } \frac{\partial \psi}{\partial n} = \hat{n}\nabla\psi \text{ is the}$

normal derivative at a boundary surface. The normal modes take the form $\psi_i(\vec{r},t) = \psi_i(\vec{r})e^{-i\omega_i t}$, where the eigenfrequencies ω_i may be degenerate, requiring additional indices to distinguish between degenerate modes.

a) Evaluate the normal modes and eigenfrequencies in a rectangular with dimensions $a \ge b \le c$.

b) Evaluate the normal modes and eigenfrequencies for a sphere of radius R.

c) Evaluate the normal modes and eigenfrequencies for a cylinder of radius R and length L.